

Global grids of gravity anomalies and  
vertical gravity gradients  
at 10 km altitude  
from GOCE gradient data  
and polar gravity



# PURPOSE

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Promote the use of GOCE products by producing (new) grids of gravity anomalies and vertical gravity gradients at 10 km altitude.

Possible improvement compared to the the HPF product of grids at zero height derived from the EGM's.

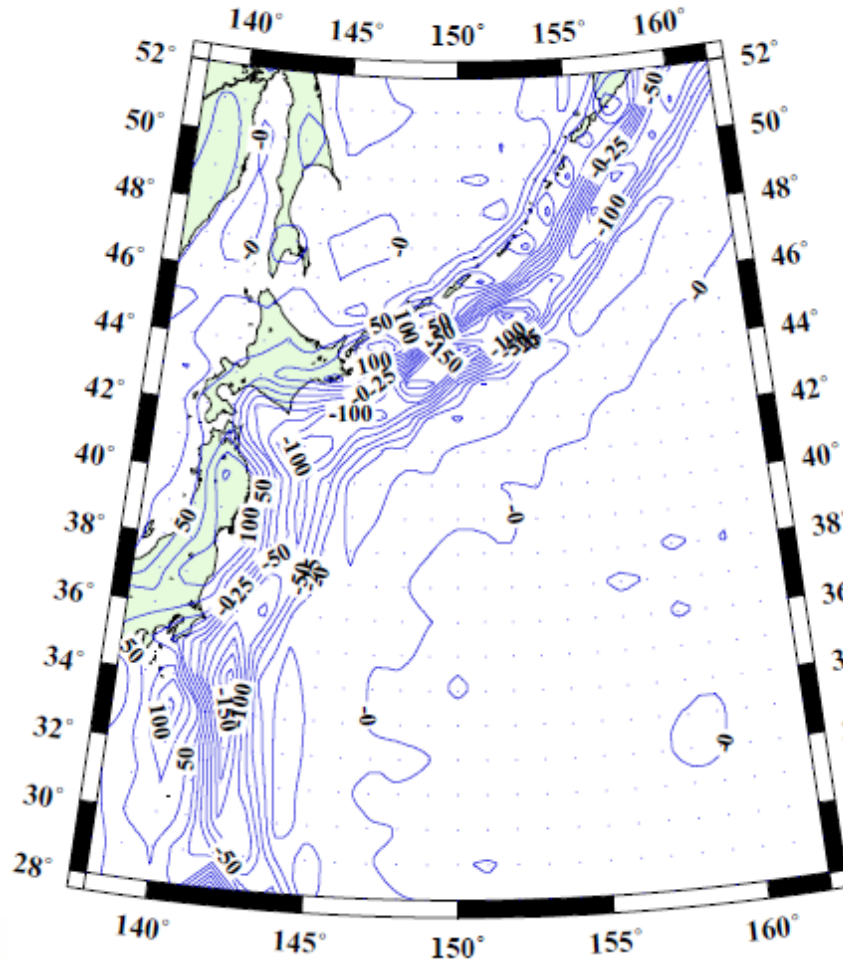
Observed gradients may contain more information than expressed through an EGM.

Grid values may be improved using polar gravity.

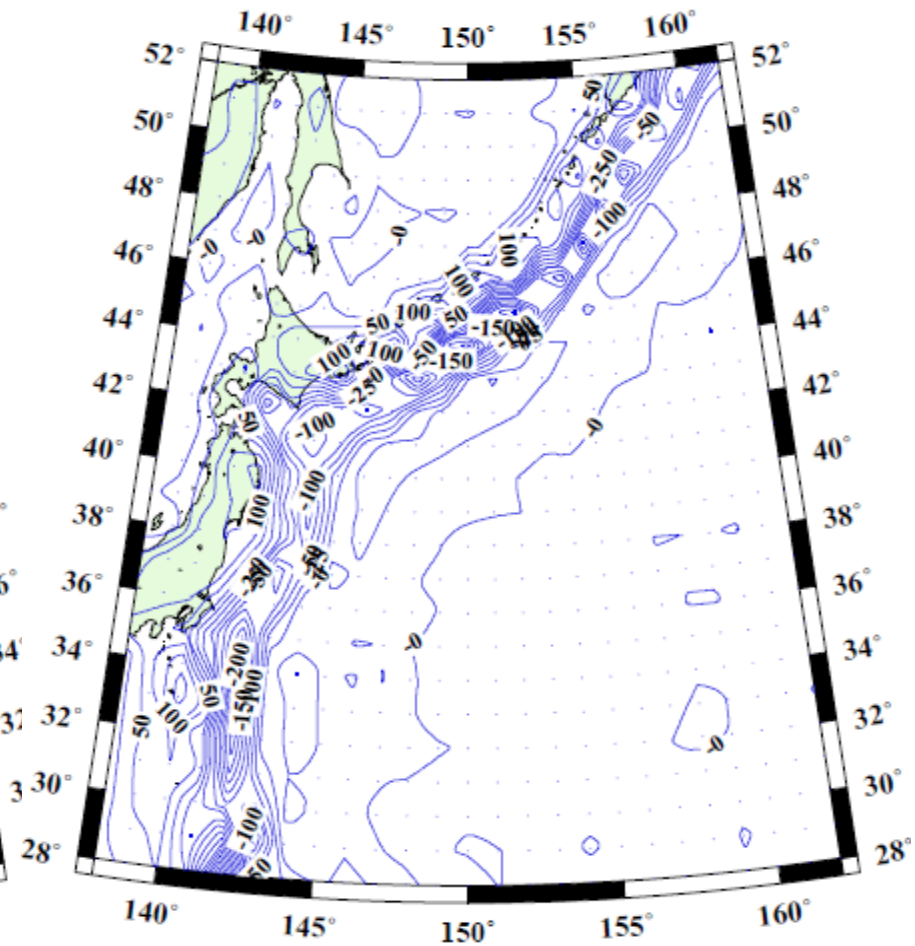


# Example of result from trench area.

dg at 10 km predicted from GOCE Tzz (mgal).



dg at 10 km computed from EGM2008 (to 510) (mgal).



## Data used.

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TRF data 2009-12, GRF data 2009-12.

Polar gravity – but not Antarctic gravity.

ITG-GRACE2010s (remove/restore)\*

EGM2008, GOCE DIR2 (control data).

Data selected closest to mid-points of 10' cells and 1/8 deg cells.\*\*

\* permits spherical approximation in local areas, help in polar caps.

\*\* nearly all cells filled !



Products: gridded gravity anomalies and vertical gradients, 10 km.

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Grids produced in 162 20x20 deg blocks with 10' spacing.

Error-estimates in grids with 1 deg spacing.



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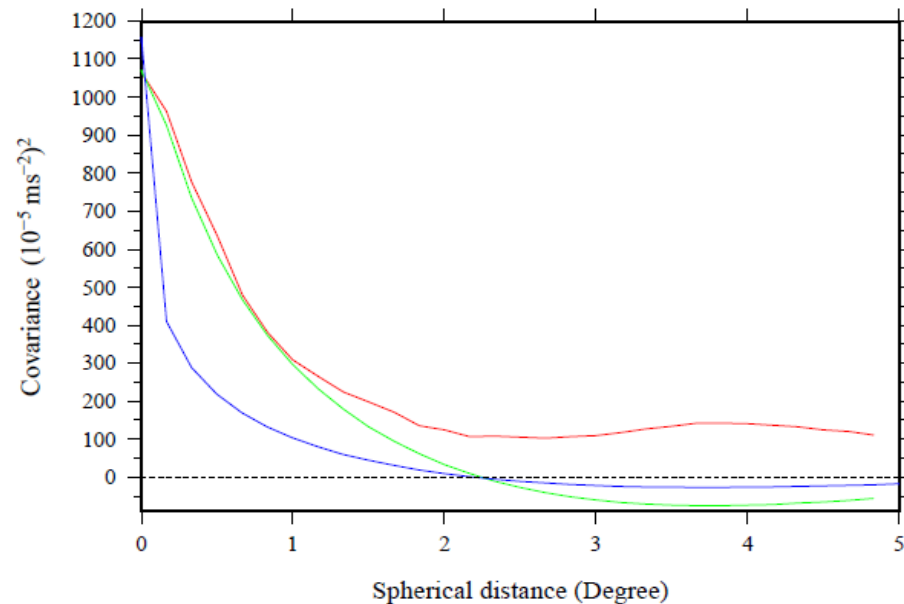
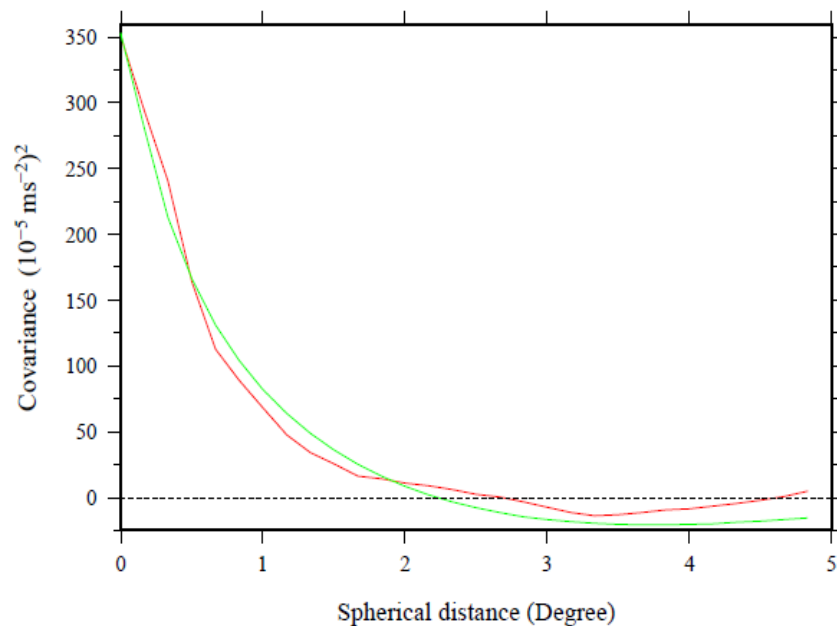
# Use of Least-Squares Collocation (LSC).

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1. Covariance estimation (from reduced data)
2. Selection of analytic representation
3. Selection of data in 25 x 25 deg. block
4. Creation of (upper triangular part of) normal equations
5. Solution of equations (Cholesky)
6. Prediction, comparison with EGM2008 to 512 and error-estimation in 1 deg. Grid.
7. Prediction of 10' grids.



## Covariance estimation (from reduced data),+analytic fitting



**Empirical (from EGM08,  $h=0$ ), analytic,**  
**Analytic from GOCE vertical gradients.**



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# Best data selection, using TRF data.

## Example of Prediction of EGM08 derived gravity anomalies at 10 km, mgal

| Number of data | Spacing (degree) | Data type       | Mean difference | Standard deviation | Mean error estimate |
|----------------|------------------|-----------------|-----------------|--------------------|---------------------|
| 22464          | 0.166            | $T_{zz}$        | -0.5            | 9.73               | 6.92                |
| 44929          | 0.166            | $T_{zz}+T_{yy}$ | -0.4            | 9.65               | 6.85                |
| 37971          | 0.125            | $T_{zz}$        | -0.5            | 9.16               | 6.79                |

$T_{zz}$  with 0.125 deg. spacing selected.



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## Computational considerations with geocol19.

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| Processor | 22    | 22    | 4     |
|-----------|-------|-------|-------|
| N         | 37971 | 22464 | 22464 |
| CH        | s     | s     | s     |
| 05        |       | 10407 | 41832 |
| 10        | 6764  | 2709  | 8381  |
| 15        | 7898  | 2962  | 7793  |
| 20        | 6966  | 2642  | 7469  |
| 25        | 7221  | 2836  | 7748  |
| 30        | 7476  | 2894  | 8300  |

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**OMP Processing time for 20x20 block, N=number of data, CH=chunk block size. Time depends on rate of disk transfer. (See Kaas et al, 2013, EGU2013).**



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# Data noise standard deviation selection

## Prediction of EGM08 derived gravity anomalies at 10 km, block 73

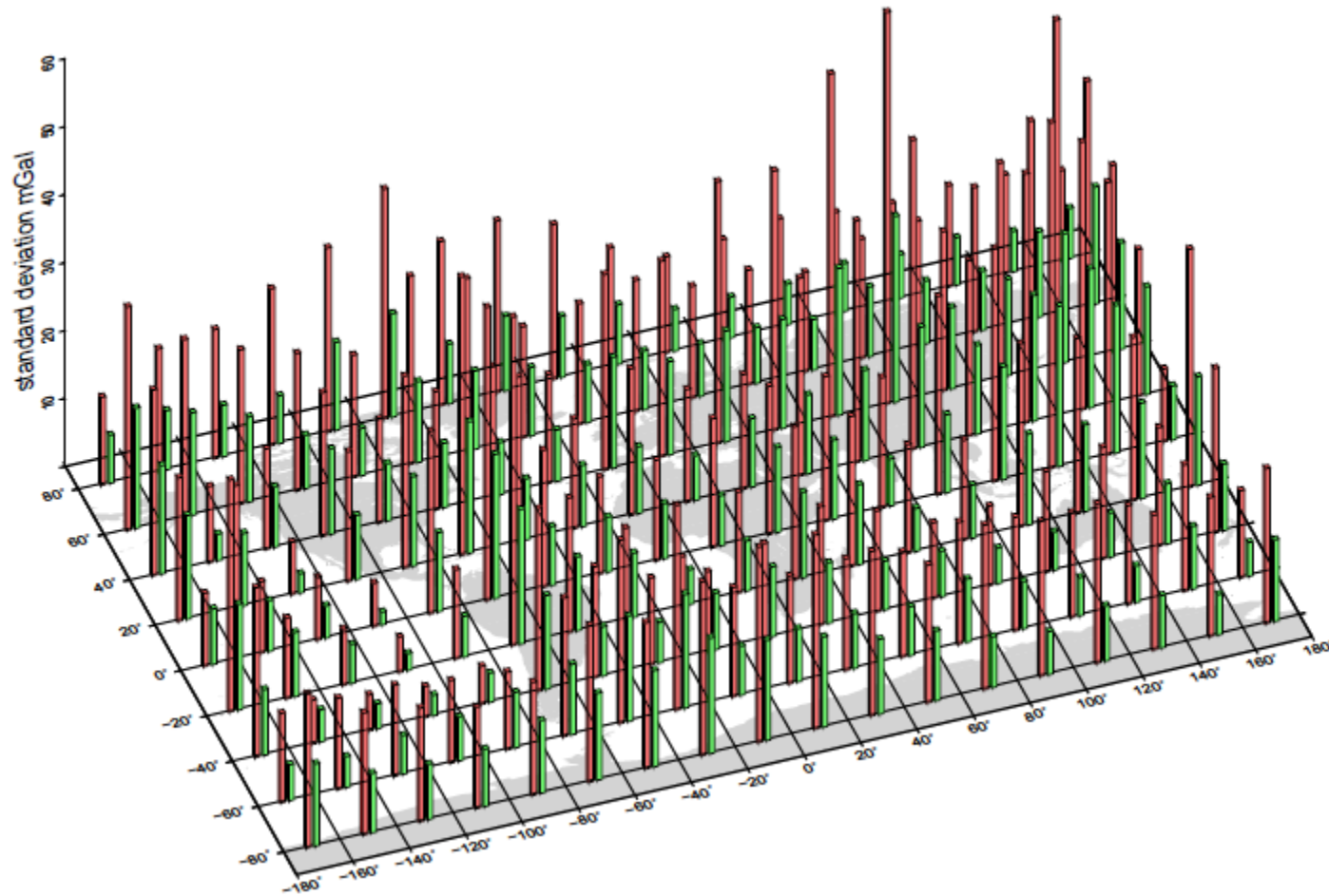
| Noise (EU) | Dg (mgal)              |                    | T <sub>zz</sub> (EU) |                 |
|------------|------------------------|--------------------|----------------------|-----------------|
|            | Observed-<br>predicted | Error<br>estimates | Observed-predicted   | Error estimates |
|            | Standard deviation     | Mean value         | Standard deviation   | Mean value      |
| 0.030      | 7.41                   | 7.67               | 3.28                 | 3.06            |
| 0.020      | <b>7.30</b>            | 7.22               | <b>3.26</b>          | 2.99            |
| 0.010      | 7.44                   | 6.52               | 3.29                 | 2.88            |
| 0.008      | 7.62                   | 6.32               | 3.33                 | 2.84            |
| 0.005      | 8.40                   | 5.75               | 3.52                 | 2.76            |
| 0.003      | 9.28                   | 5.40               | 3.77                 | 2.65            |
| EGM08-DIR2 | 7.58                   |                    | 3.53                 |                 |

**Tzz with 0.02 EU noise st.dev. selected.**

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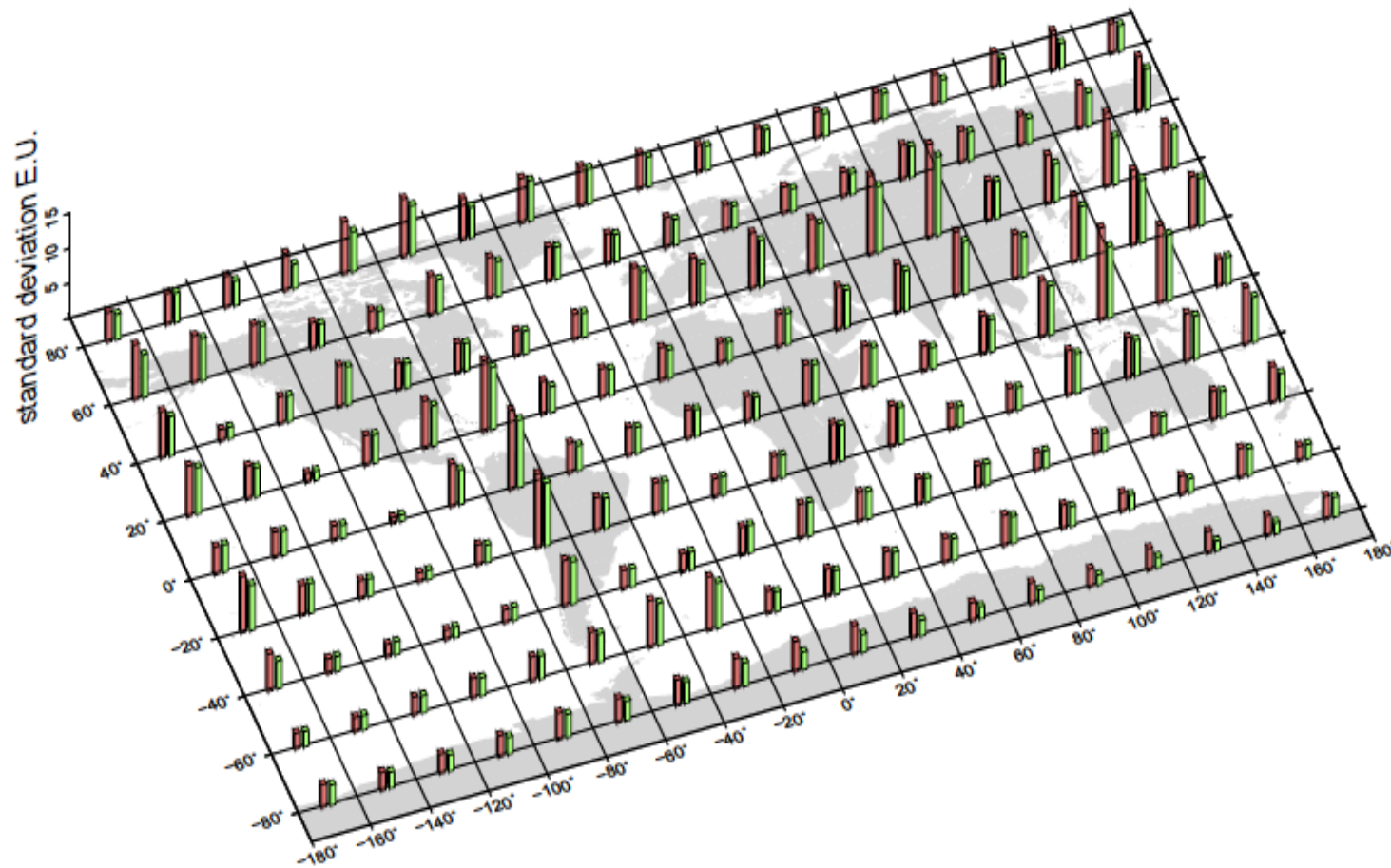
Prediction, comparison with EGM08 to 512 st.dev.  $\Delta g$ .



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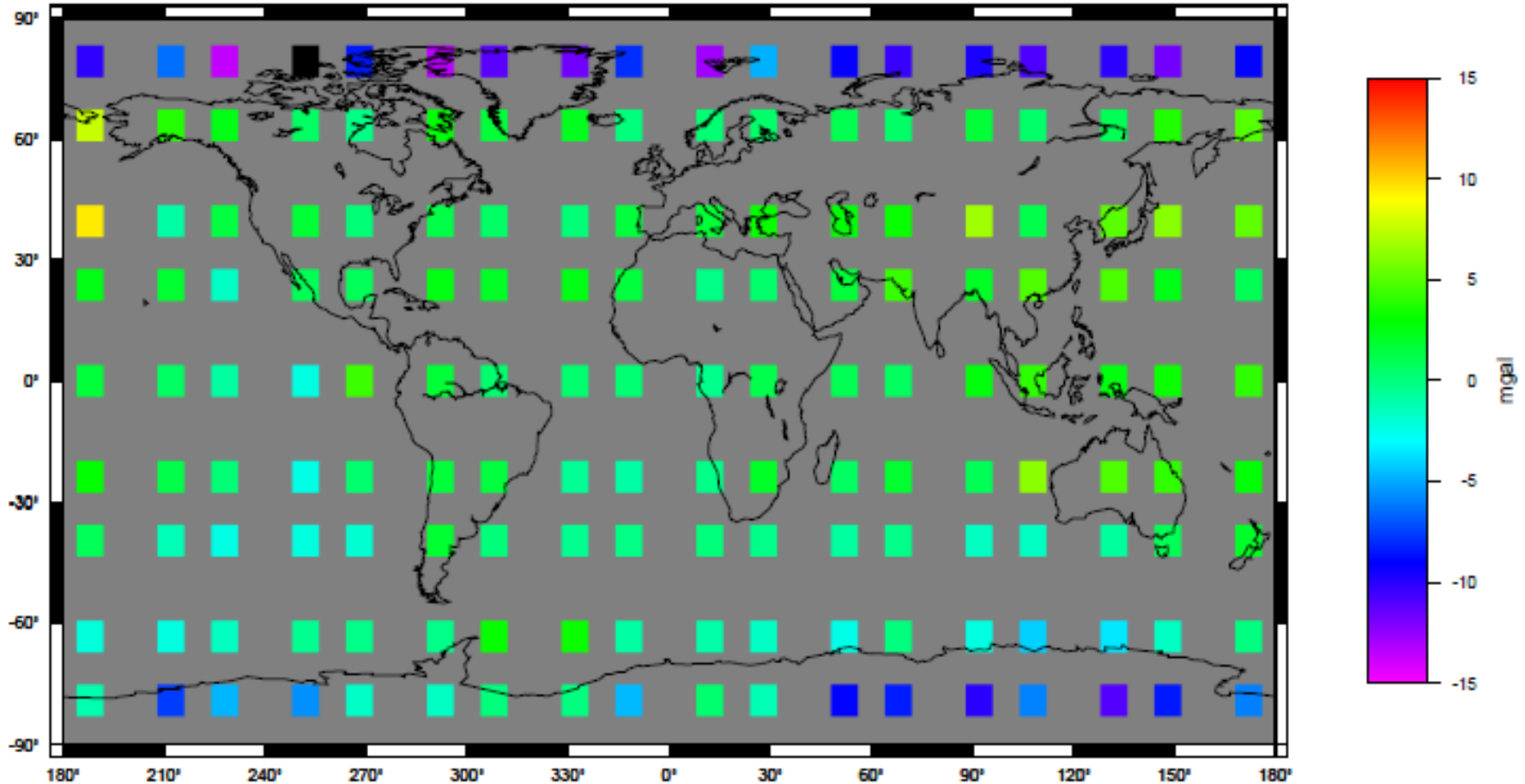
Prediction, comparison with EGM08 to 512 vert. gravity gradients (EU).



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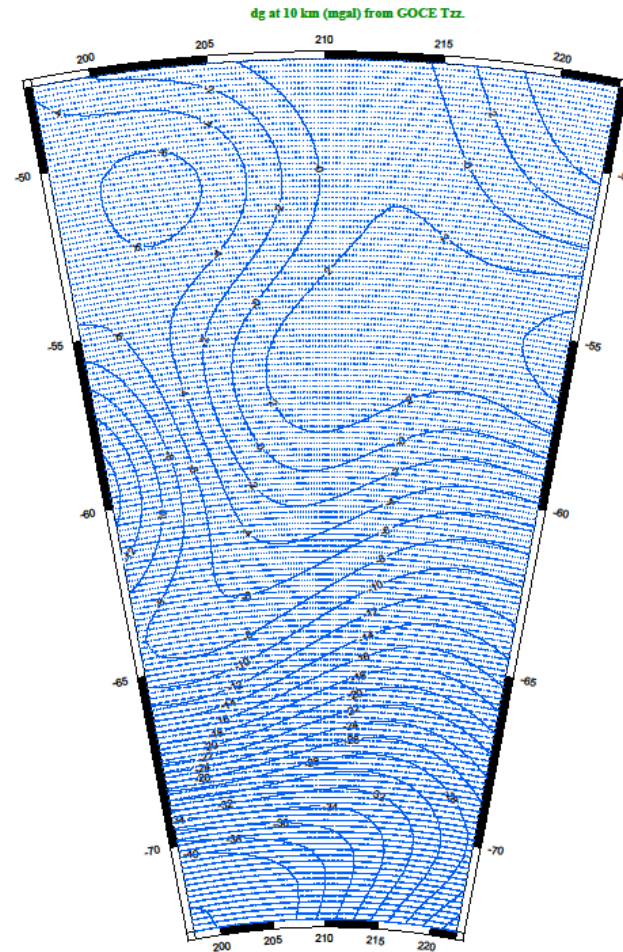
Comparison of  $\Delta g$  st.dev. differences LSC, DIR2 wrt. EGM08.  
LSC inferior at middle latitudes due to less data used (?).



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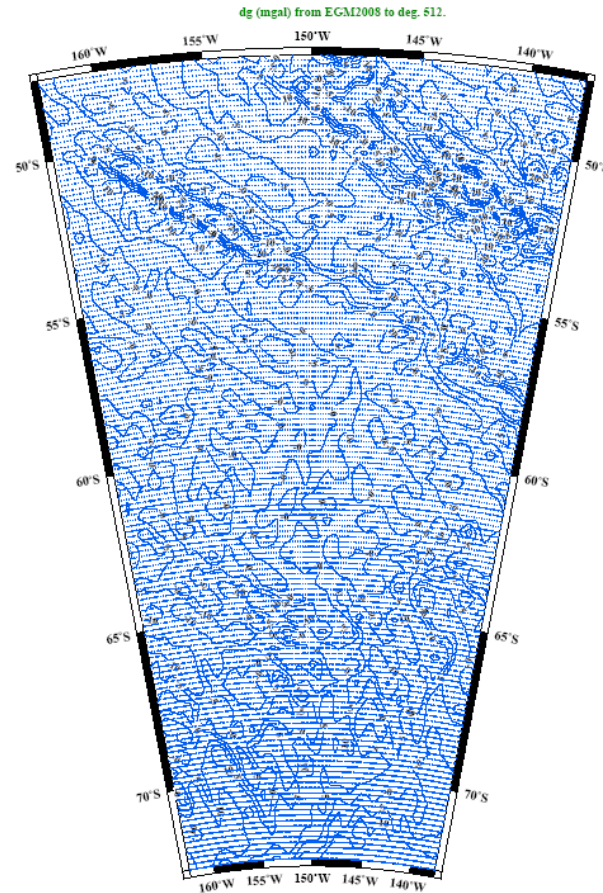
$\Delta g$  from TRF  $T_{zz}$  at 10 km (mgal).



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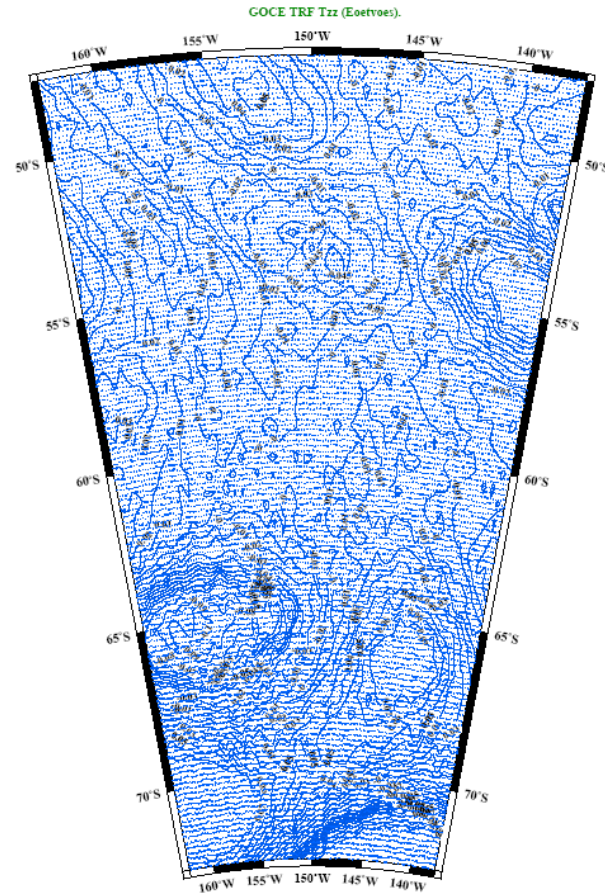
$\Delta g$  at 10 km from EGM2008 to 512 (mgal).



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# TRF $T_{zz}$ at satellite height (EU).



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## Transfer of results and further work.

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1. Grids of gravity anomalies and vertical gradients will be made available to the public by ESA.
2. Production to be repeated with POLIMI GRF data and associated error-covariance functions.
3. Using more data at middle latitudes
4. Use of MPI on several servers
5. Will the grid representation be "better" than an EGM to max. degree 240 ?

