

Global grids of gravity anomalies and vertical gravity gradients at 10 km altitude from GOCE gradient data 2009-2011 and polar gravity

D.N. Arabelos¹, M. Reguzzoni² and C.C.Tscherning³

¹ University of Thessaloniki, ² Politecnico di Milano, ³ University of Copenhagen.

Abstract: The GOCE satellite measures gravity gradients which are filtered and transformed to gradients into an Earth-referenced frame by the GOCE High Level processing Facility.

More than 32000000 data with 6 components are available from the period 2009-2011. IAG Arctic gravity project data was used north of 83 deg., while data at the Antarctic was not used due to bureaucratic restrictions by the data-holders.

Subsets of the data have been used to produce gridded values at 10 km altitude of gravity anomalies and vertical gravity gradients in 20×20 deg. blocks with 10' spacing. Various combinations and densities of data were used to obtain and compare values in areas with known gravity anomalies. The (marginally) best choice was vertical gravity gradients selected with an approximate 0.125 deg. spacing.

Using Least-Squares Collocation, error-estimates were computed and compared to the difference between the GOCE-grids and grids derived from EGM2008 to deg. 512. In general a good agreement was found, however with some inconsistencies in certain areas.

The computation time on a usual server with 24 processors was typically 50 minutes for a block with generally 40000 GOCE vertical gradients as input. The computations will be updated with new Wiener-filtered data in the near future.

1. Introduction

In order to promote the use of the GOCE gravity gradient data, new gridded products are being produced. The GOCE High Level processing Facility (HPF) has already delivered to ESA grids at ground level of gravity anomalies and geoid heights based on the global Earth spherical harmonic models (EGM). However, the original GOCE data are expected to contain information in certain areas with large gravity variations which are representing higher frequencies than those included in the GOCE EGM models. However, the existing grids at ground level are computed without taking into account the topographic masses.

Currently we have available gravity gradients which are filtered and transformed to an Earth (terrestrial) fixed frame (TRF) by HPF. We have selected the data from 2009-2011 which consist of more than 31000000 gradients, spaced along-track with approximately 7.5 km between the measurement points. These data covers the area between -83.36 deg. and 83.36 deg. latitude. Therefore ground gravity was to be used above and below these latitudes. For the Arctic the IAG has made available a dense data-set, which we used. Data are also available for the Antarctic, but the responsible (German) scientist is holding the release back.

In order not to have to take the topography into account, it was decided to create the grids at the altitude of 10 km. The grids will consist of gravity anomalies (Δg) and vertical gravity gradients (T_{zz}) and their error-estimates and have an equi-angular spacing of 10' or 0.1666 deg. Grids are produced for 20×20 deg. blocks with a 2.5 deg. border, i.e. having an extend of 25×25 deg. There are 162 of these blocks.

The method used to produce the grid-values was Least-Squares Collocation (LSC), since it permits the combination of gradient and gravity information and enables the estimation of errors; see (Torge and Müller, 2012). Also excellent results have been reported, see e.g. Tscherning and Arabelos (2011).

In the following we describe the preparations for the use of LSC and the production and quality test of the gridded values.

2. Preparations for the use of LSC

In order to eliminate long-wavelength variations and to reduce the mean values of the data in the blocks, the remove-restore procedure (Forsberg and Tscherning 1981) was used. The ITG-Grace2010s EGM (<http://www.igg.uni-bonn.de/apmg/index.php?id=itg-grace2010#content1221>) was used for this purpose to degree 36. Its contribution was subtracted from all gravity and gravity gradient data-sets and subsequently restored when necessary. The chosen maximum degree is consistent with the block size. Since no corrections are expected for the very long wavelengths from GOCE data, this implicitly means that this remove-restore procedure gives rise to a combination between GRACE and GOCE information.

Gravity anomaly data were computed in a 0.166 deg. grid at ground level from EGM2008 (Pavlis et al., 2012) and the contribution from the ITG-Grace model subtracted. This data-set was used just for covariance computation. Simultaneously data-sets of gravity anomalies and gravity gradients were created in points along the orbit as close as possible to an equi-angular grid of 0.125 deg. and 0.166 deg. spacing. T_{zz} and T_{yy} values were synthesized for the 0.125 deg. spacing, and T_{zz} and gravity anomalies selected with the 0.166 deg. spacing.

2.1 Covariance estimation and fitting with analytic models

The (reduced) EGM2008 generated ground gravity and the T_{zz} GOCE gradients were used for the estimation of the empirical covariance function, and subsequently fitted with an analytic model (Knudsen, 1987). The results using the gravity anomalies were in some cases not satisfactory (the distance to the Bjerhammarsphere too large), so the gradient data were used instead. See Fig. 1 and 2. Also Fig. 2 illustrates the different result obtained when using gravity anomalies and T_{zz} for the covariance estimation.

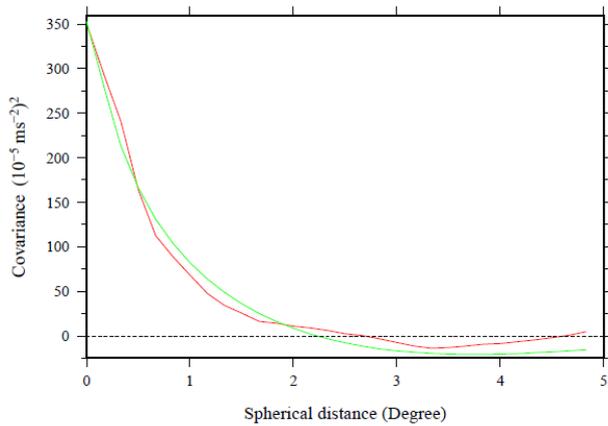


Fig.1. Example of a good fit between a local empirical (red) and an analytic (green) model.

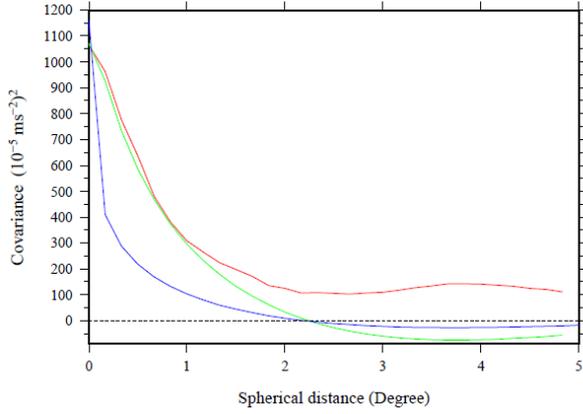


Fig. 2. Empirical (red), analytic derived from T_{zz} (blue) and analytic from gravity anomalies (green) covariance function for block 97 (western half of Australia).

The important parameters are the depth to the Bjerhammer-sphere and the variance of the (reduced) ground gravity anomalies. These values varied between 0.3 km and 50.7 km and 20 mgal² and 5055 mgal².

2.2. Control of data-error estimate

Associated with the TRF gradient data are error estimates, which for the T_{zz} values are of the order of 0.01 EU. The data are in reality along-track filtered values, but they are here used as if they were only associated with a point in space. So in order to “fix” the most appropriate error-estimate, prediction tests (comparison with EGM2008 values at 10 km) in an equatorial block (73) were performed with a sequence of different error-values, see Table 1.

Table 1. Prediction results for different values of data T_{zz} noise standard deviation and comparable values for the difference with respect to the DIR-R2 model

Noise (EU)	Δg (mgal)		T_{zz} (EU)	
	Observed-predicted Standard deviation	Error estimates Mean value	Observed-predicted Standard deviation	Error estimates Mean value
0.030	7.41	7.67	3.28	3.06
0.020	7.30	7.22	3.26	2.99
0.010	7.44	6.52	3.29	2.88
0.008	7.62	6.32	3.33	2.84
0.005	8.40	5.75	3.52	2.76
0.003	9.28	5.40	3.77	2.65
EGM08-GO_DIR2	7.58		3.53	

This made us select the value of 0.02 EU as the data.-error, hereby taking into account the representation error (but not the error-correlation).

2.3 Selection of data-type and distribution

In the above mentioned block, prediction tests performed using the 0.125 deg. and the 0.166 deg. spacing and T_{zz} and T_{yy} either simultaneously or “individually”, see Table 2.

Table 2. Result of prediction test in the block bounded by latitude -10 deg. and 10 deg., longitude 0 deg. and 20 deg. (block 73). 441 anomalous (reduced) gravity values spaced 1 deg. used for comparison generated from EGM2008-ITG-Grace. Unit is mgal.

Number of data	Spacing (degree)	Data type	Mean difference	Standard deviation	Mean error estimate
22464	0.166	T_{zz}	-0.5	9.73	6.92
44929	0.166	$T_{zz}+T_{yy}$	-0.4	9.65	6.85
37971	0.125	T_{zz}	-0.5	9.16	6.79

This made us select the T_{zz} with 0.125 deg. spacing as our basic dataset to be used to predict the grid values. However, the differences are so small, that as sequence of computations also were made with the T_{zz} data with 0.166 deg. spacing. Using this data-set reduced the computation time considerably.

2.4 Quality check

Predictions were made both in a 1 deg. grid and in a 0.166 deg. grid. In the 1 deg. grid comparisons were made with EGM2008 generated values and error-estimates were performed too. The results of the comparison using the data spaced approximately 0.166 deg. is for each grid block shown in Figs. 3 and 4. The error-estimate is not shown, since it was quite close to the standard deviation of the difference between predicted and EGM2008-ITG-Grace generated values.

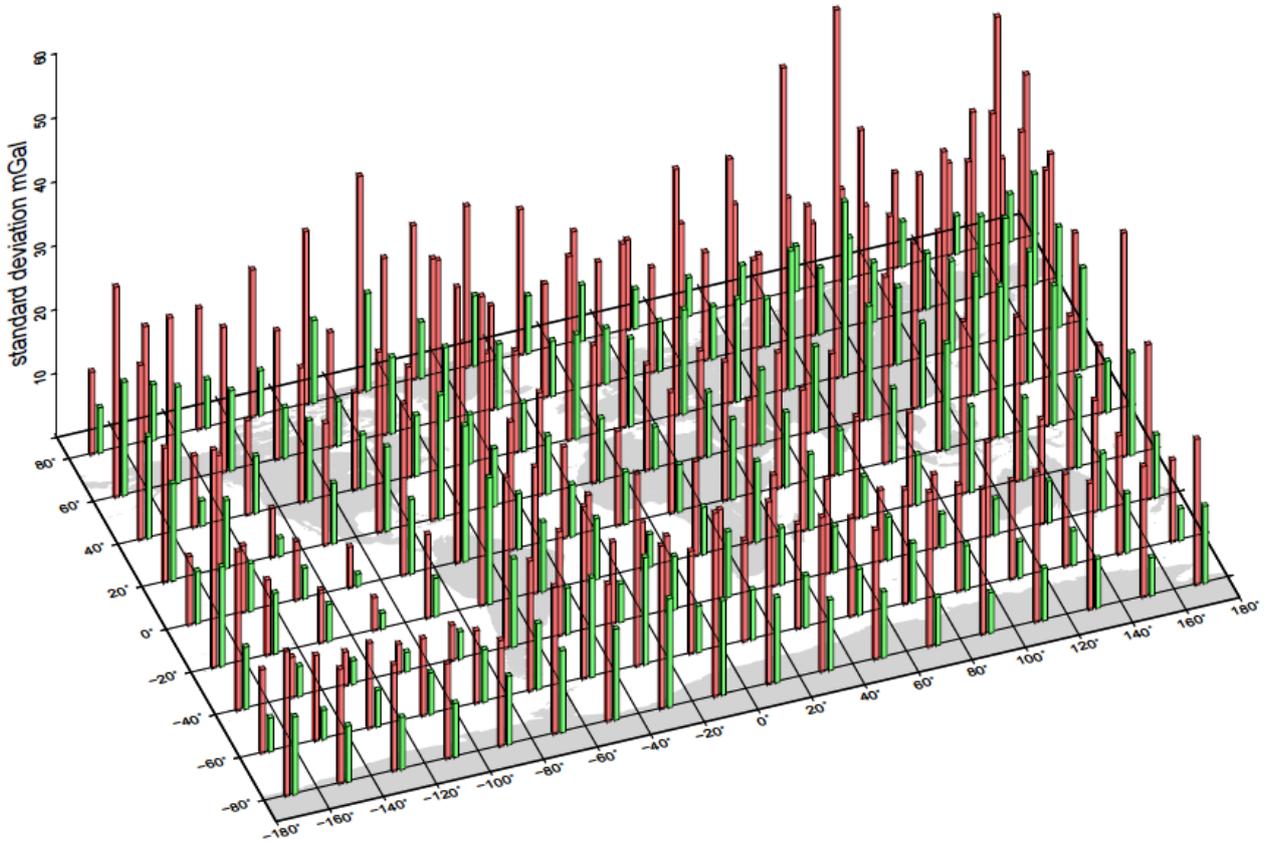


Fig. 3. Standard deviation of gravity differences (green), and of gravity (read).

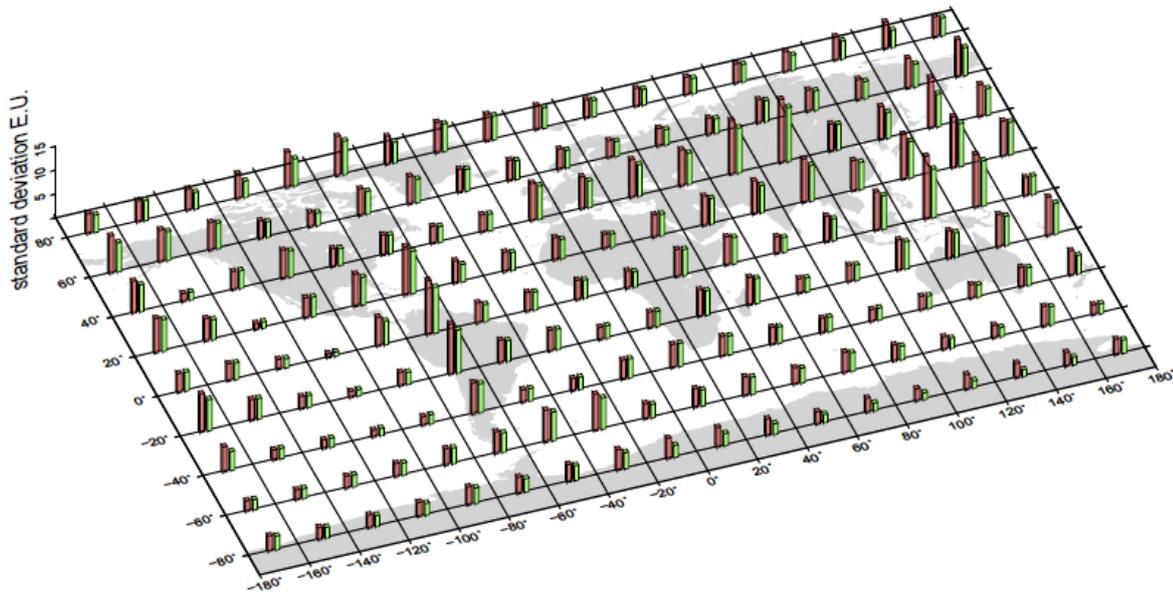


Fig. 4. Standard deviation of differences T_{zz} EGM208 minus predicted (green) and standard deviations of the EGM208 generated values (red). The large differences are caused by the use of EGM208 to degree 512 as a reference.

Comparison was also made with values generated from the GOCE DIR2 solution. The values predicted directly from the gradients had in 57 % of the blocks a smaller “error” for T_{zz} , while in 45 % of the blocks the gravity anomaly error had the smallest error when compared to EGM208. The differences are shown in Fig. 5 for gravity anomalies. Note the superior agreement using LSC at the poles..

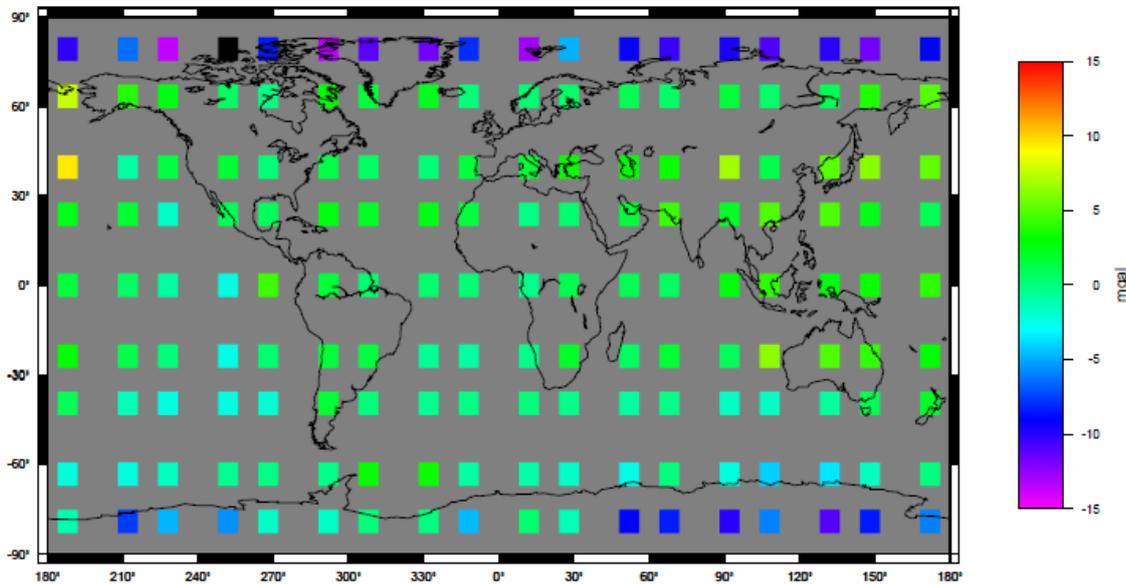


Fig. 5. Difference between standard deviations of (predicted-EGM208) and standard deviations of (DIR-R2 -EGM208) gravity anomalies at 10 km in 20 x 20 blocks.

3. Computations.

The software used (geocol19, see <http://cct.gfy.ku.dk/software/geocol19.pdf>) has been upgraded using multiprocessing, see Kaas et al. 2013. The processing depends very much on how the processors are utilized, and this again depends on how the normal-equation (upper-triangular) matrix is divided in so-called chunks. The following table illustrates the differences.

Table 3. Total processing time in seconds (s) (including error-estimation), block 73 for different chunk block sizes (CH), number of data (N) and processors.

Processors	22	22	4
N	37971	22464	22464
CH	s	s	s
05		10407	41832
10	6764	2709	8381
15	7898	2962	7793
20	6966	2642	7469
25	7221	2836	7748
30	7476	2894	8300

We are in the process of implementing Message Passing Interface (MPI), so that several computers (with several processors) can be used simultaneously.

4. Transfer of results and further work

The intension was originally to use filtered gradient data using an advanced procedure developed at POLIMI (Reguzzoni and Tselfes, 2009), but these data have not yet become available. We expect that the POLIMI data will enable us to produce improved grids, also because these values will have associated estimates of the error-correlation.

The present results are satisfactory in the sense that we for the majority of the blocks obtain a better agreement with EGM2008 of T_{zz} at 10 km when comparing with GOCE DIR-R2 values. For gravity anomalies we expect that using the POLIMI data, we can obtain a similar good agreement. Already now the differences between the results are very small, see Fig. 5.

Acknowledgement. This is a contribution to the ESA HPF.

References

- Bruinsma S.L., Marty J.C., Balmino G., Biancale R., Foerste C., Abrikosov O. and Neumayer H: GOCE Gravity Field Recovery by Means of the Direct Numerical Method, presented at the ESA Living Planet Symposium, 27th June - 2nd July 2010, Bergen, Norway;
- Forsberg, R. and C.C.Tscherning: The use of Height Data in Gravity Field Approximation by Collocation. J.Geophys.Res., Vol. 86, No. B9,pp. 7843-7854, 1981.
- Kaas. E., B. Sørensen, C. C. Tscherning, M. Veicherts: Multi-Processing Least Squares Collocation Applications to Gravity Field Analysis. Abstract and presentation at EGU2013. http://cct.gfz.ku.dk/publ_cct/cct2209p.pdf .
- Knudsen, P.: Estimation and Modelling of the Local Empirical Covariance Function using gravity and satellite altimeter data. Bulletin Geodesique, Vol. 61, pp. 145-160, 1987.
- Mayer-Guerr T., Kurtenbach E. and Eicker A: The Satellite-only Gravity Field Model ITG-Grace2010s, 2010., <http://www.igg.uni-bonn.de/apmg/index.php?id=itg-grace2010>
- Pavlis. N.K., Holmes, S.A., Kenyon, S.C. and Factor, J.K.; The development and evaluation of the Earth Gravitational Model 2008 (EGM2008) Journal of Geophysical Research: Solid Earth (1978-2012) Volume 117, Issue B4, April 2012.

Reguzzoni, M. and N.Tselfes: Optimal multi-step collocation: application to the space-wise approach for GOCE data analysis. *JGeodesy*, Vol. 83, No. 1, pp. 13-29, 2009. DOI10.1007/s00190-008-0225-x.

Torge, W. and J.Mueller: *Geodesy*, 4TH Edition, De Gruyter, 2012. ISBN: 978-3-11-020718-7.

Tscherning, C.C. and D.Arabelos: Gravity anomaly and gradient recovery from GOCE gradient data using LSC and comparisons with known ground data. Proc. 4th International GOCE user workshop, 31 March - April 1, 2011. ESA SP-696, 2011.